

# Graph Network Surrogate Model for Optimizing the Placement of Horizontal Wells for CO<sub>2</sub> Storage

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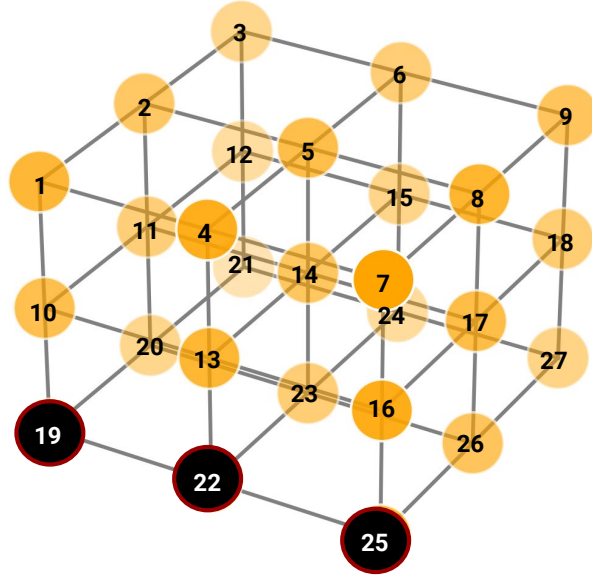


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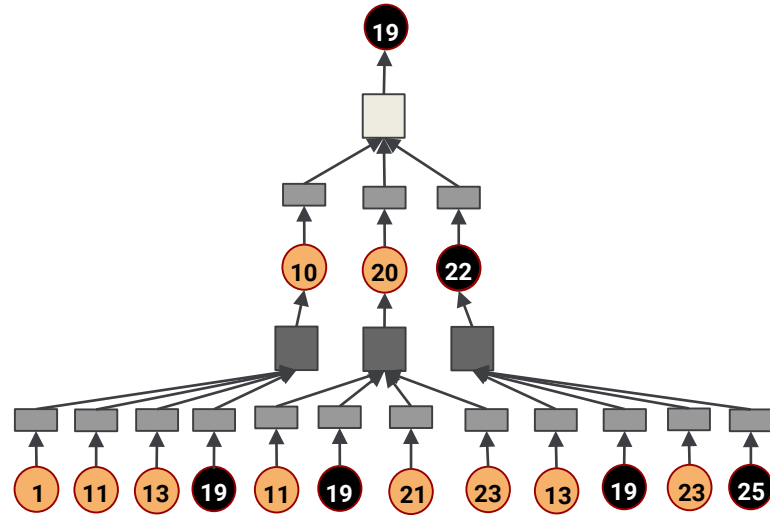
# General Motivation

- ❑ Well placement optimization is often performed using population-based stochastic search algorithms (e.g., particle swarm optimization, genetic algorithms, differential evolution)
- ❑ These optimizations are computationally expensive due to the large number (~1000s) of simulation runs required
- ❑ Reduced-order/surrogate models can greatly improve optimization efficiency, but challenges exist for cases with changing well locations
- ❑ Here we use graph neural networks, with separate networks to predict global pressure and saturation, and a third network for bottom-hole pressure

# 3D Graph & Computational Graph



Graph



# of Message Passing Layers = 2

# Input Features for GNN

- ❑ Edge features: transmissibility and geometric quantities
- ❑ Node features
  - Current pressure & saturation ( $P_0, S_0$ )
  - Permeability ( $k$ )
  - Depth ( $d$ )
  - Porosity ( $\phi$ )
  - Well index of the cell ( $WI$ )
  - Injection mass rate by perforation ( $q_{inj}$ )
  - One hot encoding for different types of nodes ( $e$ )
  - Current time step length ( $\delta t$ )

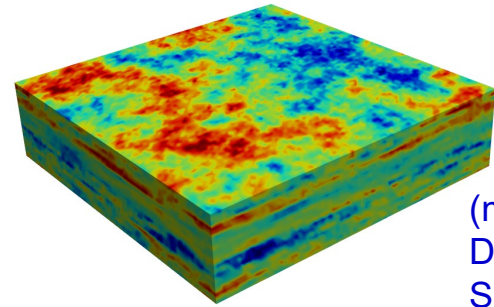
# 3D Geological Carbon Sequestration

## □ Model parameters

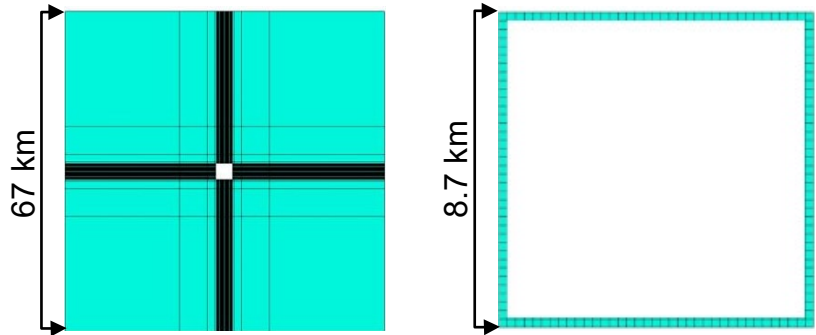
- Mt. Simon formation (Illinois Basin)
- 82 x 82 x 20 grid (134,480 cells, structured grid)
- 8.5 km x 8.5 km x 122 m
- 4 horizontal injectors
- Each well injects 0.5 Mt/year for 20 years
- Using Eclipse 300 CO2STORE for training runs

## □ Deep-learning setup

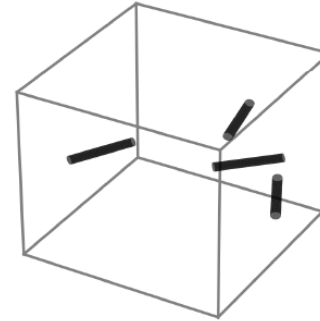
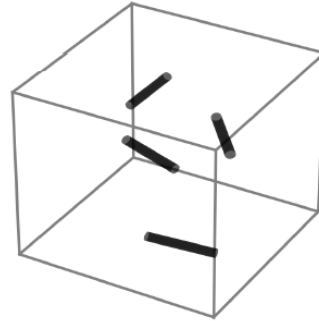
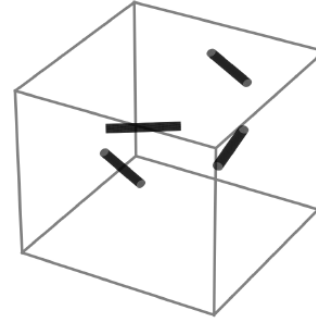
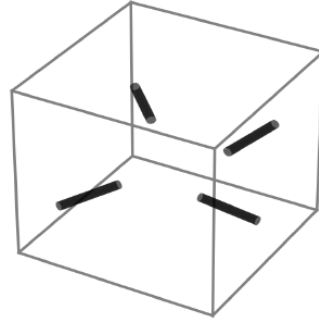
- 200 simulations with **random horizontal well configurations (4 wells in each case)**
- 100 for training, 50 for validation, 50 for testing
- Median errors for test set: 4% for pressure and 6% for saturation



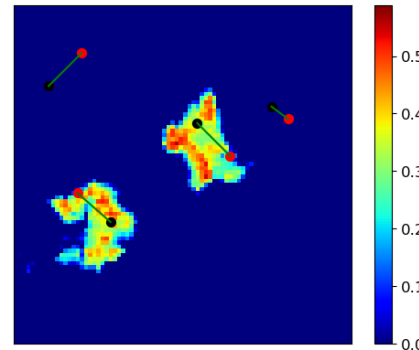
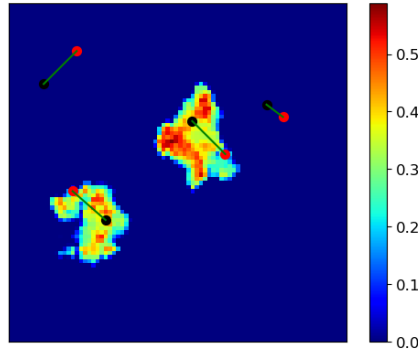
(model from  
Dylan Crain,  
Su Jiang)



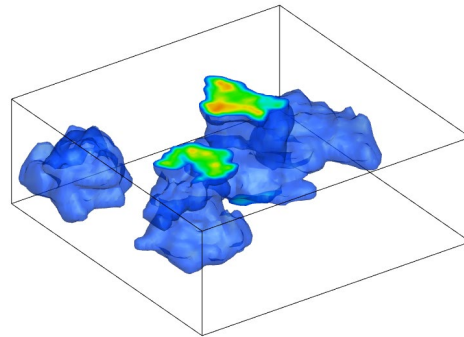
# Horizontal Well (Random) Configurations



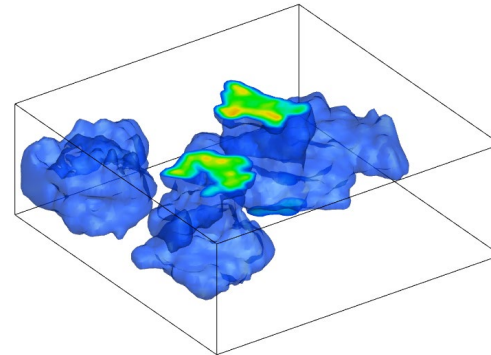
# Test Case with $P_{50}$ Error Saturation at 20 years (10 Steps)



(wells projected onto top layer)

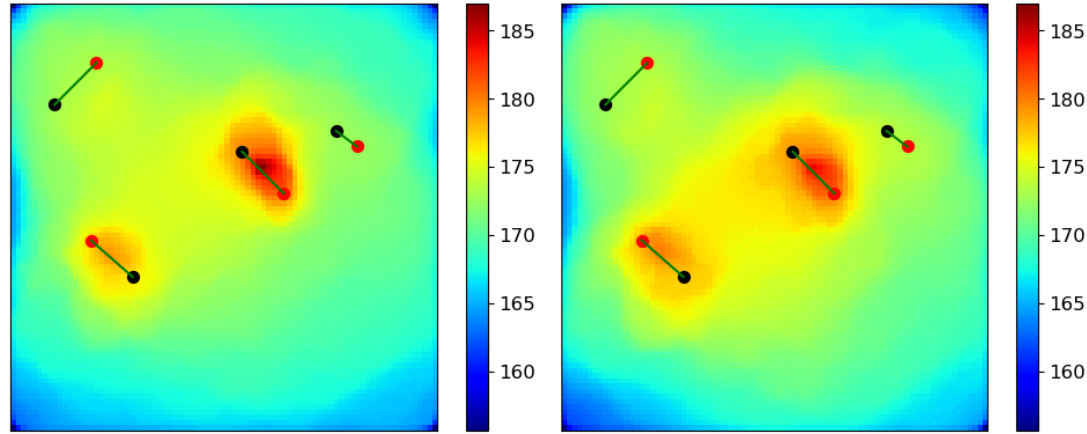


Simulation



GNSM

# Test Case with $P_{50}$ Error Pressure at 20 years (10 Steps)



Simulation

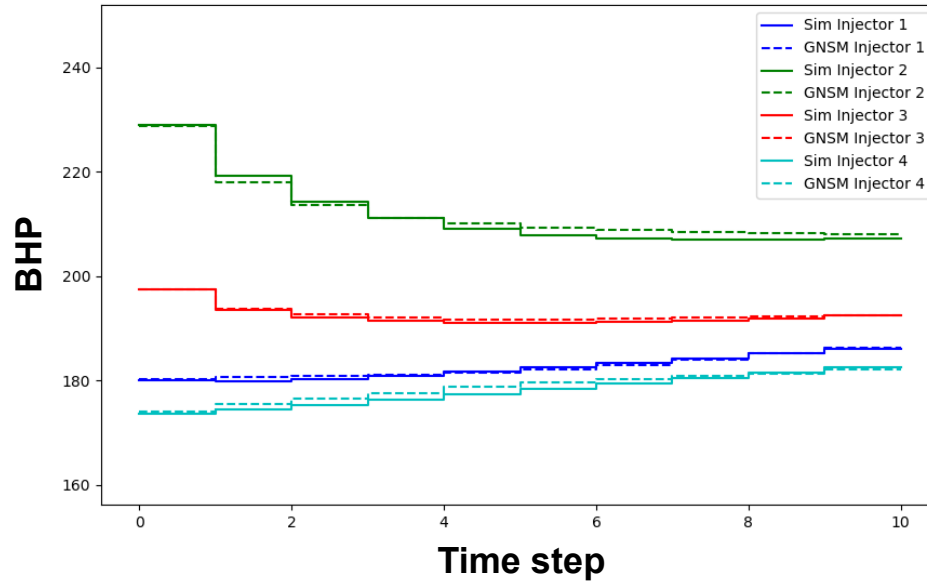
GNSM

(wells projected onto top layer)



# P<sub>50</sub> Error Test Case

## Bottom-hole Pressures

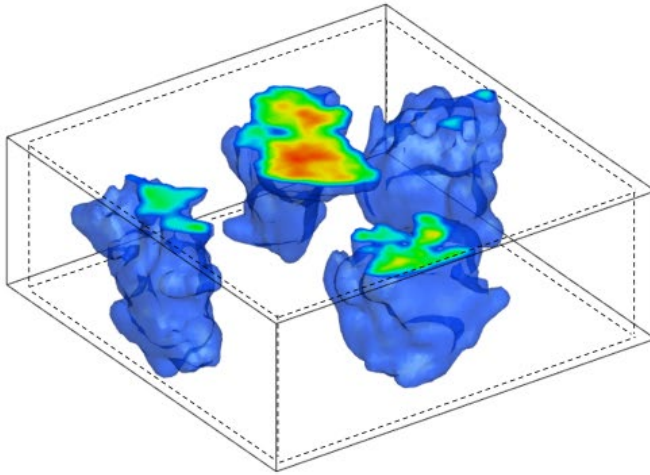


# Footprint Ratio Calculation

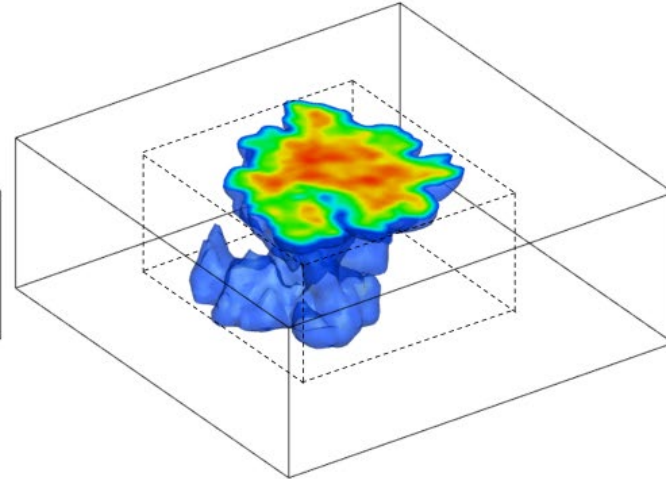
$$R_{fp}^i = V_{fp}^i / V_{tot}$$

$V_{fp}^i$  : CO<sub>2</sub> footprint (at 20 years) for test case  $i$

$V_{tot}$  : total bulk volume of storage aquifer



**Example 1**



**Example 2**

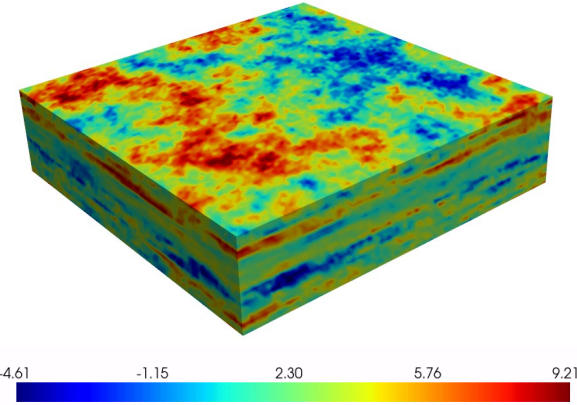
# Optimization Setup

## □ Simulation parameters

- Optimize locations of four horizontal injectors to minimize the CO<sub>2</sub> footprint ratio
- Well geometric constraints (in table)
- Maximum BHP (276 bar) and CO<sub>2</sub> retention constraints
- Run for 20 years (ECLIPSE CO2STORE)

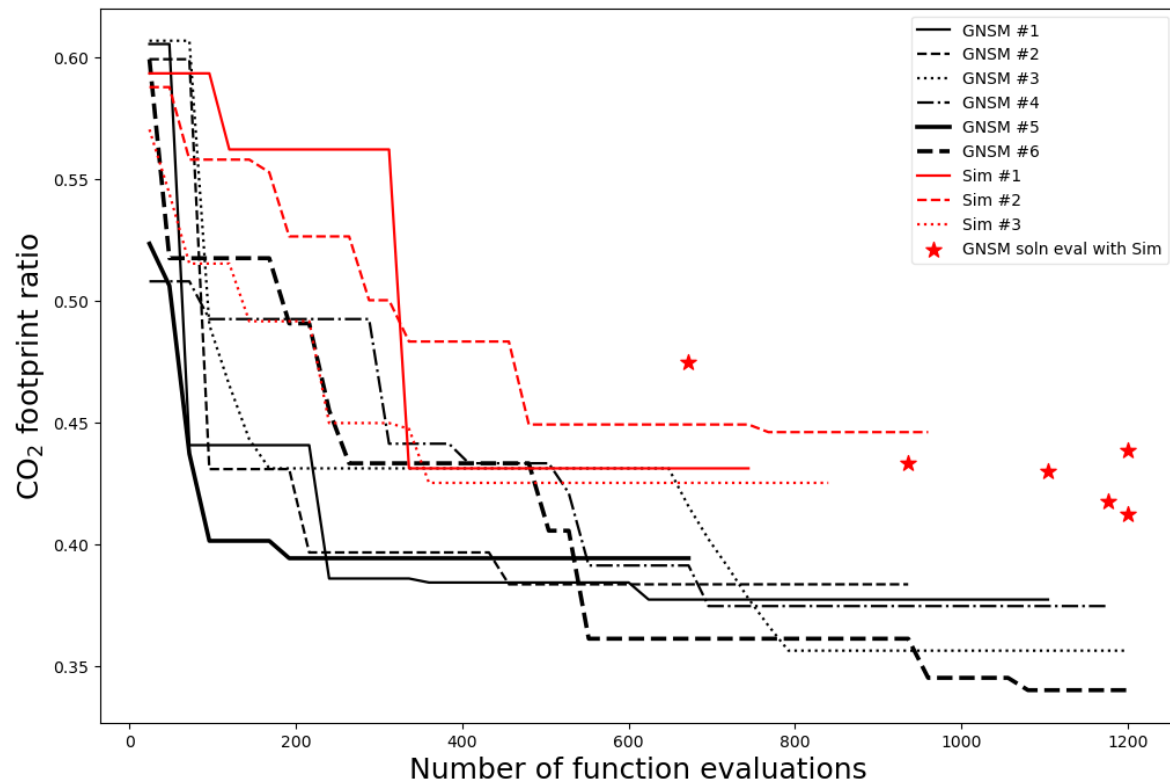
## □ Optimization setup

- Optimization method: differential evolution
- Population size: 24
- Terminate when obj. fcn. change is less than 1% over 20 iterations, or after 50 iterations



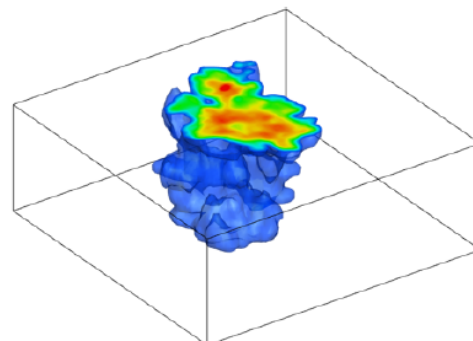
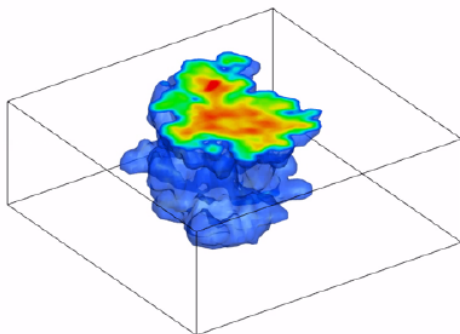
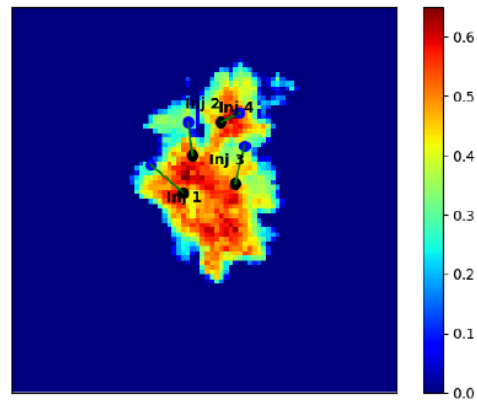
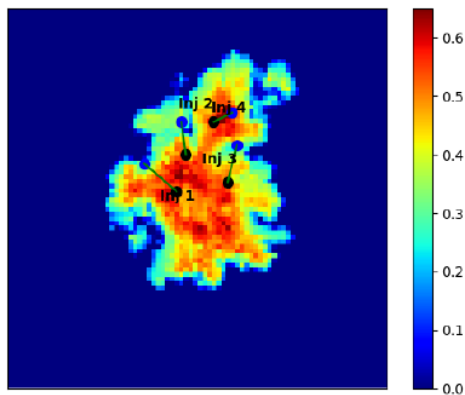
No.	Constraint type	Number
1.	Maximum well length	1200 m
2.	Minimum well length	480 m
3.	Minimum interwell distance	720 m
4.	Minimum well-to-boundary distance	424 m
5.	Maximum heel-to-toe difference in depth	0 m

# Progress of Optimizations



- GNSM speedup ~120x
- 6 GNSM runs versus 3 simulation-based opt runs
- Best GNSM run outperforms best simulation-based run

# Optimized CO<sub>2</sub> Footprint



**Simulation (w/ opt well locations from GNSM run)**

**GNSM**

# Summary & Current Work

- ❑ Developed a graph network surrogate model for 3D CCS problem with changing horizontal well locations
- ❑ Achieved reasonable accuracy for global pressure and saturation states and for well bottom-hole pressures
- ❑ Applied the GNSM for well placement optimization with constraints; achieved ~120x speedup in DE optimization runs
- ❑ *Currently investigating extrapolation to new geomodels, considering other network architectures like graph transformers and graph U-Net*

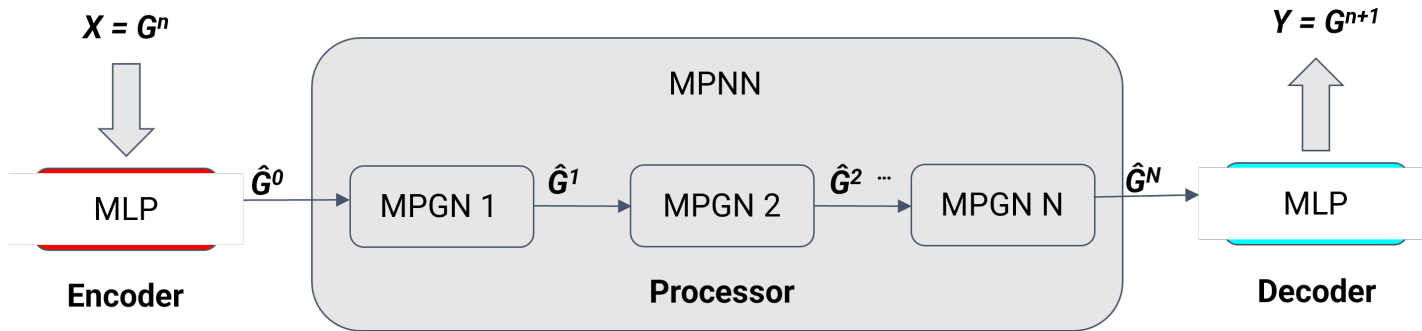
# Acknowledgements

- ❑ BHP (through GeoCquest II), Stanford Smart Fields Consortium, Stanford Center for Carbon Storage
- ❑ Oleg Volkov, Su Jiang, Dylan Crain, Amy Zou
- ❑ SDSS Center for Computation

# Backup Slides



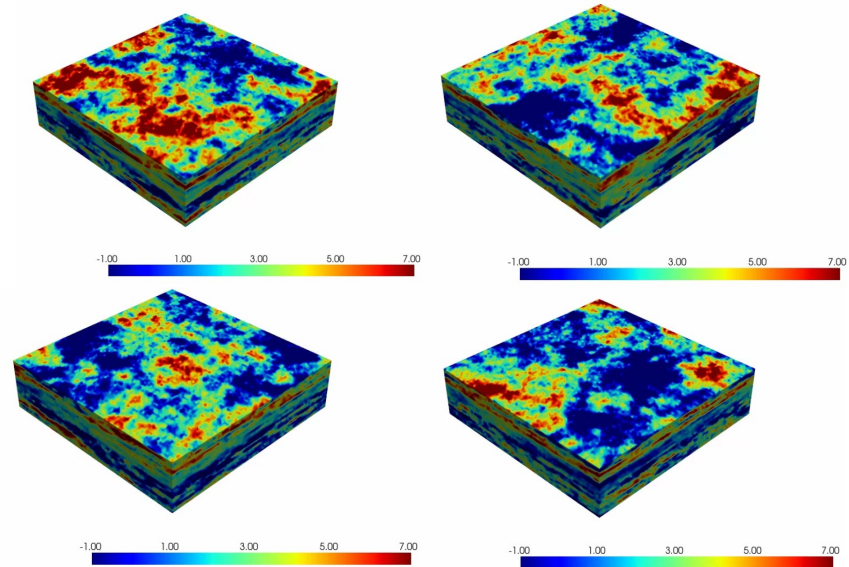
# GNN Model Architecture



- $X$  : input to the **encoder** (multilayer perceptron, MLP)  
 $G^n$  : current state graph (including node and edge features)
- $G^0$  : current encoded graph and input to the **processor**  
 $G^i$  : output of message passing graph network  $i$  (MPGN)
- $Y$  : output of the **decoder** (MLP)  
 $G^{n+1}$  : predicted future state graph (pressure/saturation at next time step)

# New Realizations – Extrapolation Test

- ❑ Different permeability & porosity fields
- ❑ Deep-learning setup
  - **No retraining**
  - 100 test case configurations each



# Errors for State Variables

## New Realizations (1–3)

