

## Probabilistic Assessment and Uncertainty Quantification of a Geothermal Resource, Red River Formation, North Dakota

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### ABSTRACT

Geothermal energy stands out as a sustainable green energy that complements the global energy transition away from fossil fuels. The immense potential of geothermal resources in deep sedimentary basins in North Dakota makes it an attractive and alternative source of energy. Effective utilization of geothermal resources requires a good understanding of inherent uncertainties and variabilities. This study incorporates the application of geo-statistical methods on geothermal reservoir engineering principles for evaluating uncertainty parameters within a geothermal reservoir. Uncertainty analysis quantifies the variability and ambiguity of subsurface parameters to better evaluate resource utilization and project feasibility. This study accounts for uncertainties in field data inputs from the Red River Formation that are essential to assess the geothermal energy potential, reduce risk associated with geothermal energy exploration and promote sustainable development. Probabilistic assessment and uncertainty quantification of geothermal resources are crucial in informed decision making and successful reservoir utilization. In this study of the Beaver Lodge field in the Red River Formation, we found that arithmetic means for total geothermal resources, aquifer geothermal resources and producible geothermal resources are:  $4.0 \times 10^{18}$  J,  $2.5 \times 10^{17}$  J and  $4.8 \times 10^{16}$  J respectively. We found that relative impact plot shows total geothermal resource is sensitive to the gross thickness and volume of the reservoir, aquifer geothermal resource is sensitive to the porosity and water saturation of the reservoir and lastly, the producible geothermal reservoir is sensitive to the fluid flowrate and formation permeability.

### 1. INTRODUCTION

#### 1.1 Geothermal energy in North Dakota

Geothermal energy is a clean and sustainable energy source that uses the thermal properties of the earth's crust to generate energy for heating and cooling as well as electricity generation. Primordial heat produced billions of years ago and radioactive decay are the main sources of this energy. It is divided into two categories: moderate to low temperature resources ( $< 150^{\circ}\text{C}$ ), which are typically found in deep sedimentary strata or shallow subsurface rocks, and high temperature resources ( $> 150^{\circ}\text{C}$ ), which are found in areas of significant tectonic activity (Dickson et al., 2004). This heat can be used for various applications, including electricity generation and direct heating. Geothermal energy is estimated to currently supply, for direct heat use and geothermal heat pumps, approximately 21,700 TJ/yr (6029 GWh/yr) of energy through direct-heat applications in the United States (Ufondu, 2017). Geothermal energy in North Dakota, particularly in the western region, has significant potential for electricity generation and heating. Several empirical correlations have been utilized for permeability modelling and heat flow studies have been done on the Red River Formation to highlight the geothermal potential (Gyimah et al., 2023a). Machine learning has been used to improve subsurface characterization within the Red River Formation to classify it as a geothermal hotspot (Koray et al, 2023). The state's favourable conditions for Enhanced Geothermal Systems (EGS) are being explored using data from deep oil wells (Ouadi et al, 2023). The deeper formations of the Williston basin have been estimated to have high geothermal resource systems and great geothermal storage systems (Gyimah et al, 2023b) (Gosnold et al, 2017) (Vashaghian et al, 2023). From Merzoug's studies on existing oil and gas wells, they could be repurposed in North Dakota to geothermal wells (Merzoug et al, 2023). Geothermal heat pumps are increasingly used in homes, schools, and public buildings to provide efficient heating and cooling. Geothermal resources in the Williston Basin in North Dakota occur as thermal waters in at least four regional aquifers, i.e., the Inyan Kara (Cretaceous), Madison (Mississippian), Duperow (Devonian), and Red River (Ordovician). According to the U.S. Energy Information Administration (EIA), exploration and production risk stands out as a pivotal factor contributing to the gradual development of Enhanced Geothermal Systems (EGS) resources (Lowry et al, 2016). Mufer et al, 1978 employed a volumetric approach coupled with probabilistic analysis to calculate the thermal energy content and analyze the recoverable energy for electricity generation. In a study focused on the Dikili-Izmir region in Turkey, Turan et al, 2021 conducted probabilistic heat in place calculations, revealing that there is a 50% probability of generating 75 MW of net electrical power. Wang et al, 2022 ingeniously constructed proxy numerical models utilizing Experimental Design and Response Surface Methodology in conjunction with the Monte Carlo Simulation technique. Their approach provided a probabilistic assessment of the thermal energy potential in the Maichern Sag area in South China.

## 1.2 Red River Formation

The Red River Formation in the Williston Basin of North Dakota has a thickness of over 214m, temperatures exceeding 140°C and its permeability is 0.1–38 mD (Hartig, 2018). The formation is divided into upper and lower subunits. The lower subunit makes up two thirds of the Red River portion in the middle basin and is composed of fossiliferous wackestone that has been burrow-mottled. Towards the margins of the basin, the lower Red River becomes less fossiliferous, less burrow-mottled, and grades into dense dolostone. The lithologies of each upper Red River cycle are as follows, in ascending order: nodular to laminated anhydrite, laminated microcrystalline dolostone, burrowed lime mudstone to fossil wackestone, and a thin argillaceous dolomitic mudstone (Sippel, 1998). The Red River Formation has excellent potential projected to produce  $3.4 \times 10^{22}$  J of thermal energy (Porro and Augustine 2014).

## 2. METHODOLOGY

### 2.1 Reservoir Parameters Determination

From the North Dakota Industrial Commission (NDIC), reservoir core data were collected for the Beaver Lodge field as shown in Tables, 1, 2 and 3. The mean and standard deviation were calculated from five wells and were used as representative reservoir variables for probabilistic assessment and uncertainty quantification. The representative reservoir variables are crucial in characterizing the subsurface reservoir of the Beaver Lodge field within the Red River Formation. The parametric probabilistic method which works on the principle for statistical distribution was used to generate the expectation curve and uncertainty quantification. Typically, probabilistic assessment and uncertainty quantification methods have been applied on oil and gas reserves (Asante et al, 2021; Ampomah et al, 2016; Morgan et al, 2021).

### 2.2 Probabilistic method for Geothermal Resource

This paper seeks to quantify the geothermal resource and analyze the uncertainties within the Beaver Lodge field in the Red River Formation in North Dakota. The geothermal resource quantified is sub-divided into three categories: total geothermal resource, aquifer geothermal resource and producible geothermal resource. Probabilistic method can handle large and complex dataset and engineering problems. The parametric method is an analytical procedure that utilizes the mean and standard deviation to generate probabilistic outcomes and uncertainty results. The methodology for the parametric method is displayed in Fig. 1. After generating the mean and standard deviation for the reservoir variables, the first step for the parametric method is to convert them into lognormal mean and lognormal standard deviation. The geothermal resource in lognormal forms is then summed up for lognormal mean and lognormal variance to generate the probabilistic outcome.

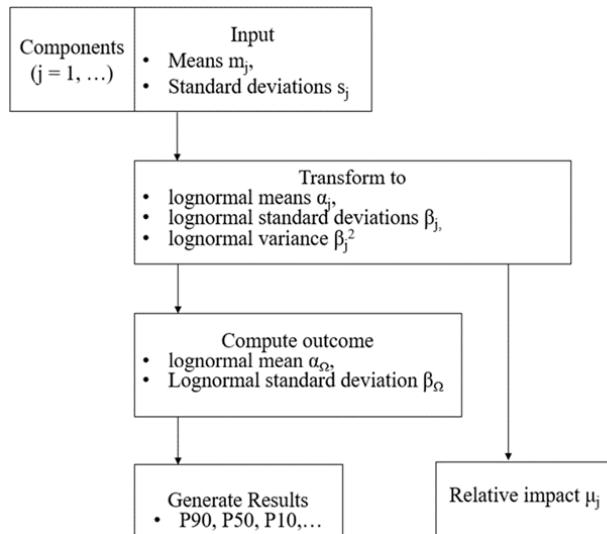


Figure 1: Flow chart for Probabilistic methods

Reservoir Variable	Mean	Standard deviation
Area ( $m^2$ )	52609133	0
Gross thickness (m)	205.435	28.65
Density ( $kg/m^3$ )	2600	100
Temperature ( $^{\circ}C$ )	150	10
Heat capacity (J/kg/K)	950	30

**Table 1: Reservoir Variables for Total Geothermal Resource**

Reservoir Variable	Mean	Standard deviation
Area ( $m^2$ )	52609133	0
Gross thickness (m)	205.435	28.65
Density ( $kg/m^3$ )	2600	100
Temperature ( $^{\circ}C$ )	150	10
Heat capacity (J/kg/K)	950	30
Water saturation (stb/rb)	0.73	0.05
Porosity	0.084	0.0086

**Table 2: Reservoir Variables for Aquifer Geothermal Resource**

Reservoir Variable	Mean	Standard deviation
Area ( $m^2$ )	52609133	0
Gross thickness (m)	205.435	28.65
Density ( $kg/m^3$ )	2600	100
Temperature ( $^{\circ}C$ )	130	10
Heat capacity (J/kg/K)	950	30
Water saturation (stb/rb)	0.73	0.05
Porosity (frac.)	0.084	0.0086
Flow rate ( $m^3/h$ )	0.223	0.068

**Table 3: Reservoir Variables for Producible Geothermal Resource**

$$V_j = s_j/m_j \quad (1)$$

Where  $V_j$  is the coefficient of variation,  $s_j$  is the standard deviation and  $m_j$  is the mean.

$$\beta^2 = \ln(1 + V_j^2) \quad (2)$$

Where  $\beta^2$  is the lognormal variance.

$$u_j = \beta_j^2 / \sum \beta_j^2 \quad (3)$$

Where  $u_j$  is the Relative impact

$$\alpha_j = \ln(m_j) - 0.5 \times \beta_j^2 \quad (4)$$

Where  $\alpha_j$  is the lognormal mean

$$P90 = \exp(\alpha - 1,281\beta) \quad (5)$$

Where P90 is the Probability at least 90%

$$P50 = \exp(\alpha) \quad (6)$$

Where P50 is the Probability at least 50%

$$P10 = \exp(\alpha + 1,281\beta) \quad (7)$$

Where P10 is the Probability at least 10%

$$E_P = \rho c_p v q \Delta T (T_f - 20^\circ\text{C}) \quad (8)$$

Where  $E_P$  is the Producible geothermal resource,  $\rho$  is density ( $\text{kg}/\text{m}^3$ ),  $c_p$  is heat capacity ( $\text{J}/\text{kg}/\text{K}$ ),  $v$  is volume ( $\text{m}^3$ ),  $q$  is flowrate ( $\text{m}^3/\text{h}$ ),  $T_f$  is the reservoir fluid temperature ( $^\circ\text{C}$ ) and  $T_a$  is annual mean temperature ( $^\circ\text{C}$ ).

$$E_A = \phi \rho S_w c_p v \Delta T (T_f - T_a) \quad (9)$$

Where  $E_A$  is the Aquifer geothermal resource,  $S_w$  is water saturation and  $\phi$  is porosity (frac)

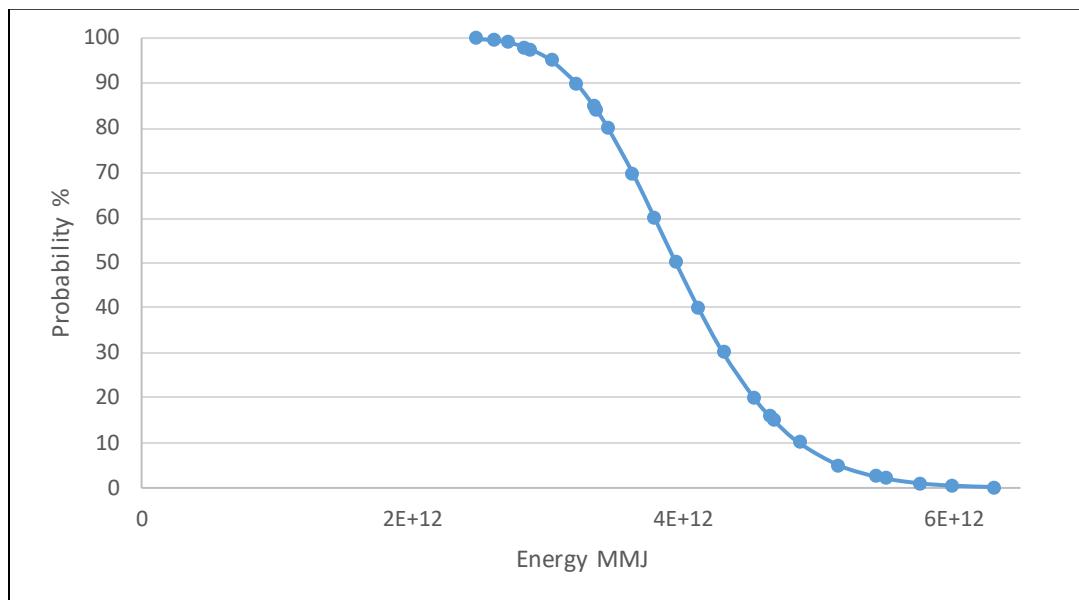
$$E_T = \rho c_p v \Delta T (T_f - T_a) \quad (10)$$

Where  $E_T$  is the Total geothermal resource

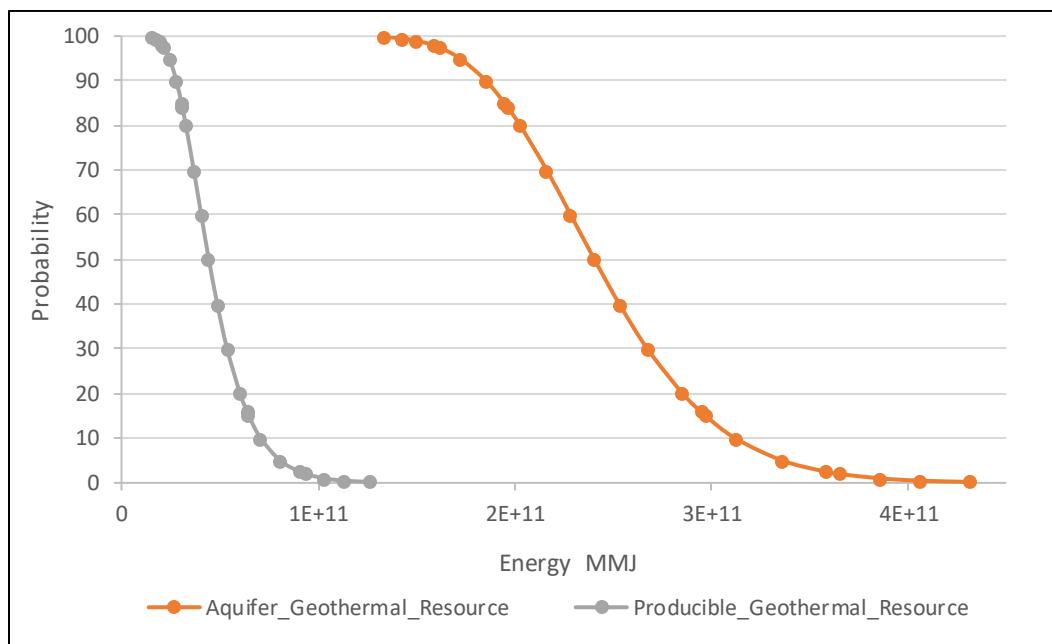
### 3. RESULTS AND DISCUSSION

#### 3.1 Probabilistic assessment of geothermal reservoir parameters

From the expectation curve, probabilistic estimation of geothermal energy details large accessible energy output within the subsurface of the Red River Formation. As expected, the total geothermal resource which is the energy within the formation is the largest followed by the aquifer geothermal resource and lastly the producible geothermal resource, shown in Fig. 2 and Fig. 3. The aquifer geothermal resource refers to the energy from only the formation fluid therefore its lower energy output compared to the total geothermal resource. The producible geothermal resource is the energy practically utilized at the surface after considering heat loss and fluid flow rate, hence the lowest energy output. For P90 of total, aquifer and producible geothermal resource are:  $3.2 \times 10^{18}$  Joules,  $1.9 \times 10^{17}$  and  $2.7 \times 10^{16}$  respectively. For P50 of total, aquifer and producible geothermal resource are:  $3.9 \times 10^{18}$  Joules,  $2.4 \times 10^{17}$  and  $4.4 \times 10^{16}$  respectively. For P10 of total, aquifer and producible geothermal resource are:  $4.8 \times 10^{18}$  Joules,  $3.1 \times 10^{17}$  and  $7 \times 10^{16}$  respectively. From our studies on the Beaver Lodge field in the Red River Formation, the arithmetic mean for total geothermal resources, aquifer geothermal resources and producible geothermal resources are:  $4.0 \times 10^{18}$  J,  $2.5 \times 10^{17}$  J and  $4.8 \times 10^{16}$  J respectively.



**Figure 2: Probabilistic Expectation Curve for Total Geothermal Resource, Beaver Lodge field**



**Figure 3: Probabilistic Expectation Curve for both Aquifer Geothermal Resource and Producible Geothermal Resource, Beaver Lodge field**

### 3.2 Uncertainty and relative impact of geothermal reservoir parameters

From the relative impact plot of the reservoir variables, we are able to quantify the uncertainty for the geothermal resource. Firstly, the total geothermal resource has gross thickness (74%) as the most contributing factor to uncertainty followed by temperature (17%), density (6%) and heat capacity (4%) respectively, Fig. 4. This shows the essence of areal extent and thickness collectively bulk volume in determining the total geothermal resource. The Aquifer geothermal resource has its uncertainty outcome as gross thickness (47%), porosity (25%), water saturation (11.4%) and temperature (10.7%), Fig. 5. Since fluids occupy the porous spaces within the formation, water saturation and porosity are sensitive factors to the aquifer geothermal resource. Lastly, producible geothermal resource has its uncertainty outcome dominated by the fluid flowrate (68%), then gross thickness (15%), Fig. 6. Fluid flowrate within subsurface of formation depends on the formation permeability, thereby highly permeable formations allow fluids to flow through quickly.

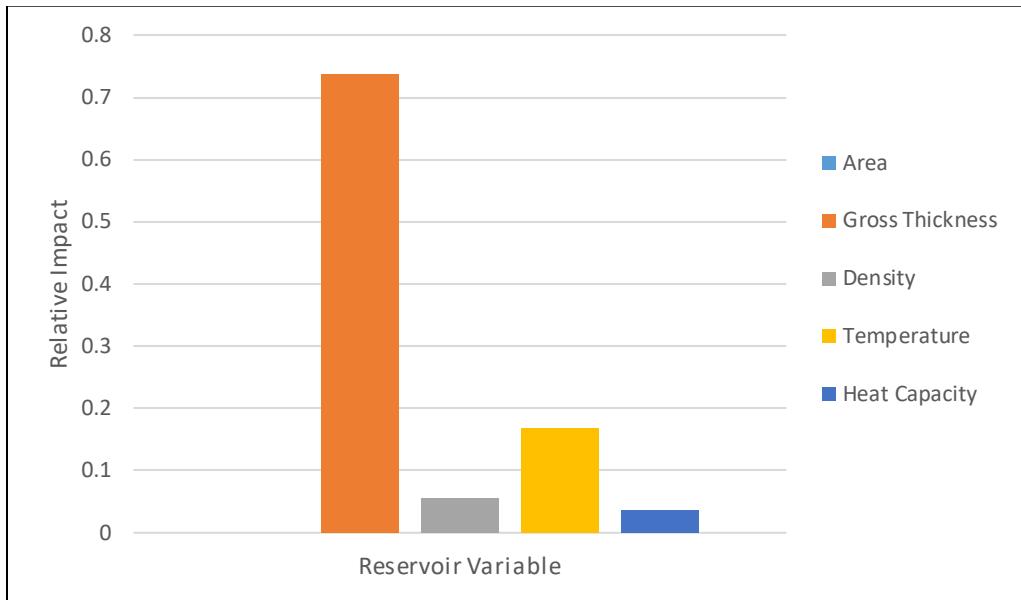


Figure 4: Relative Impact Plot for Total Geothermal Resource, Beaver Lodge field

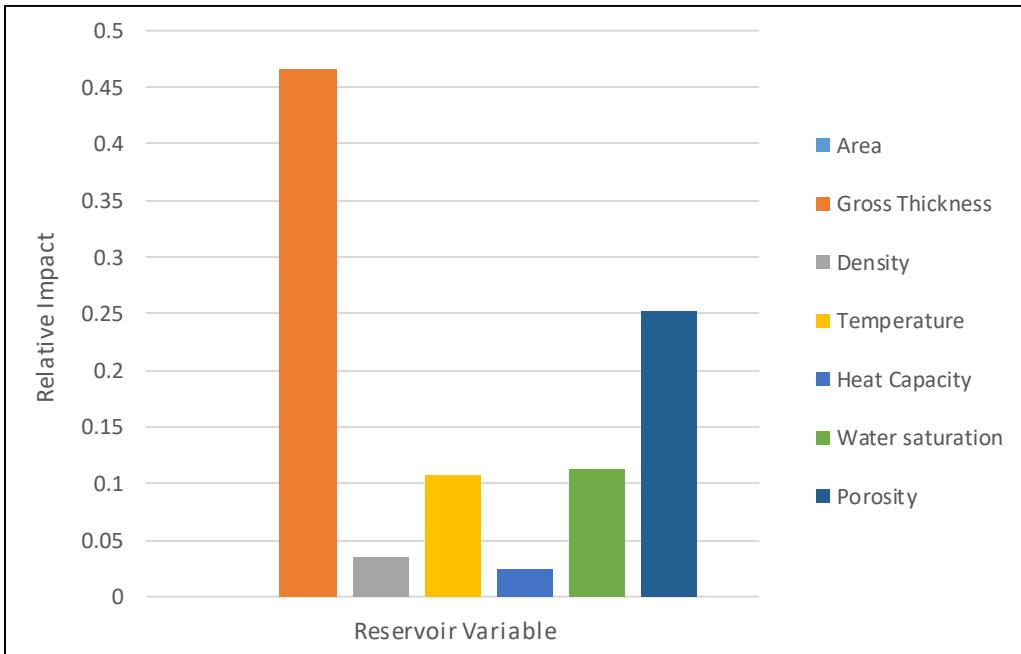
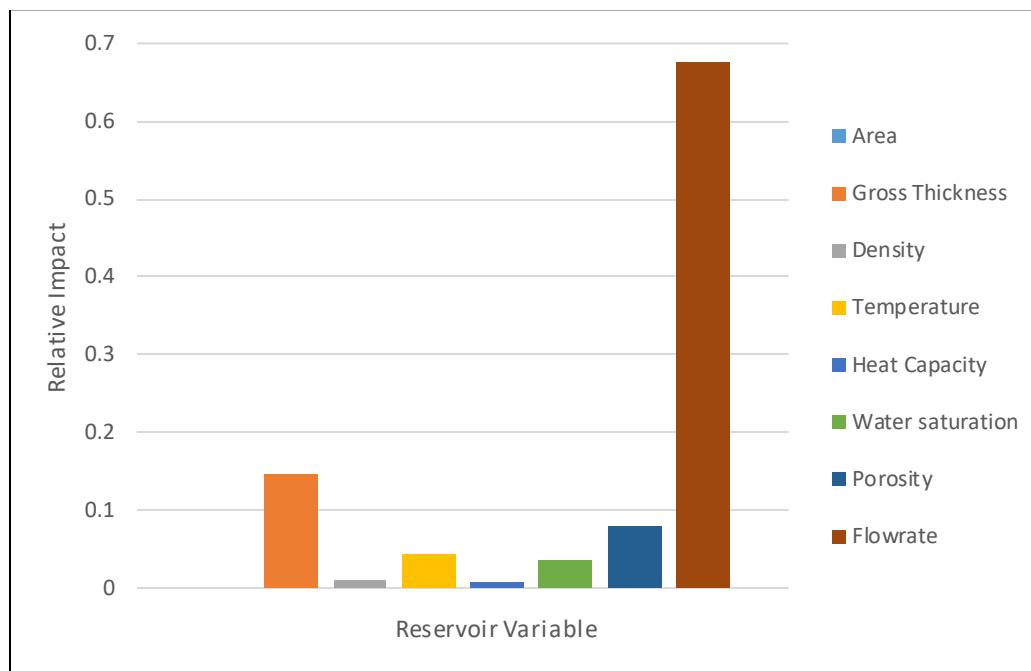


Figure 5: Relative Impact Plot for Aquifer Geothermal Resource, Beaver Lodge field



**Figure 6: Relative Impact Plot for Producible Geothermal Resource, Beaver Lodge field**

#### 4. CONCLUSIONS

Geothermal energy, a sustainable and large untapped energy resource was estimated in large energy quantities within the Red River Formation in the Williston Basin. From the probabilistic method (parametric), geothermal energy output was estimated for total geothermal resource, aquifer geothermal energy and producible geothermal resource. Large energy reserves within the Formation in the form of geothermal energy are accessible to the energy industry. From the relative impact plot, sensitive reservoir variables are depicted to assist in decision making for future viable projects. The geothermal energy assessment provides notable information for resource potential and quantification. The probabilistic method (parametric) was successfully used to estimate the geothermal resource and its sensitive reservoir variables. The quantification of geothermal reserves is very complex due to uncertainty with data precision and heterogeneity hence probabilistic method is another technique utilized to quantify project feasibility and total uncertainty. To conclude, exploration of the geothermal resource within the Williston basin would boom the energy industry.

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